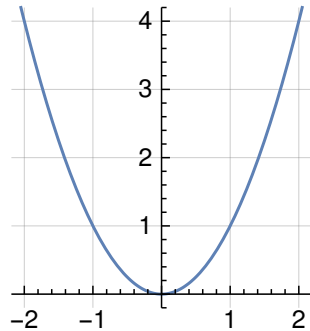
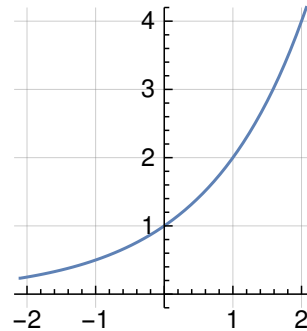


1. Let $f(x) = x^2$ and $g(x) = 2^x$, whose graphs are given below.

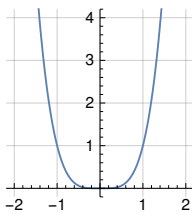


$$f(x) = x^2$$

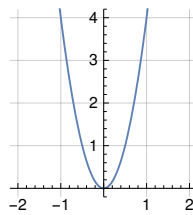


$$g(x) = 2^x$$

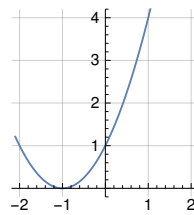
(a) Identify each of the following graphs with the functions below them.



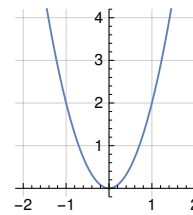
$f(x + 1)$



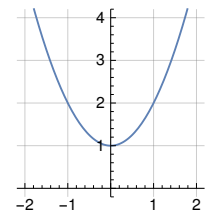
$f(x) + 1$



$2f(x)$

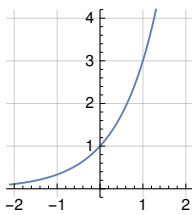


$f(2x)$

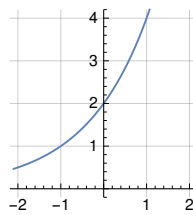


$f(x)^2$

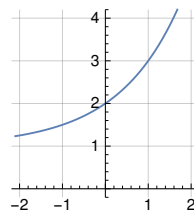
(b) Identify each of the following graphs with the functions below them.



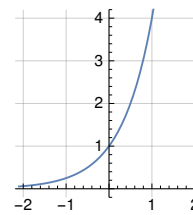
$g(x + 1)$



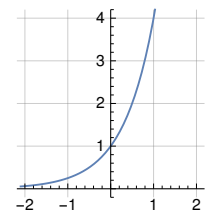
$g(x) + 1$



$2g(x)$

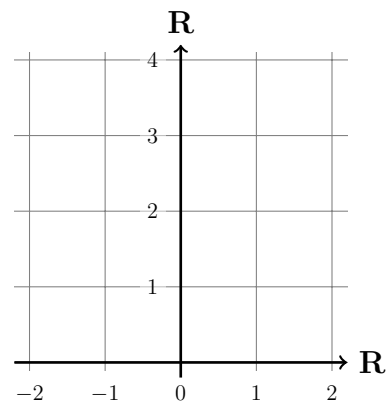
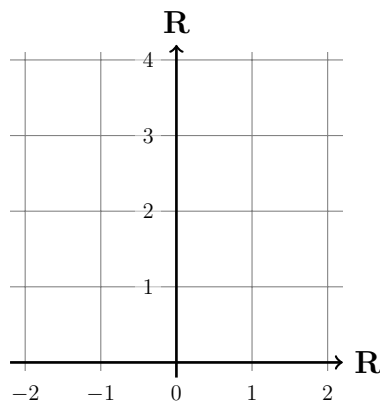


$g(2x)$

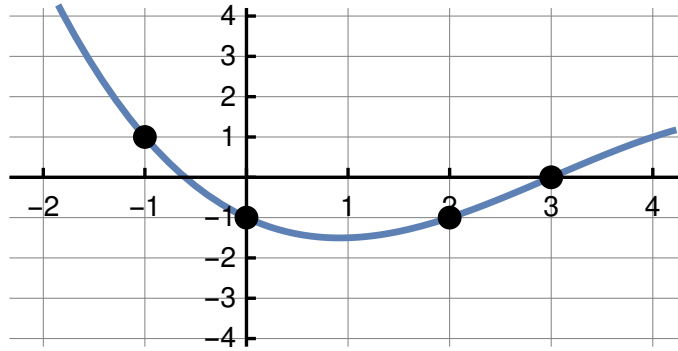


$g(x)^2$

(c) Draw $f(x + 1)^2 + 1$ on the left, and $g(x + 1)^2 + 1$ on the right.

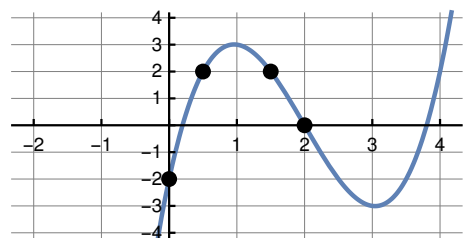
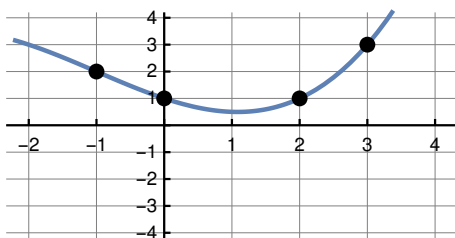
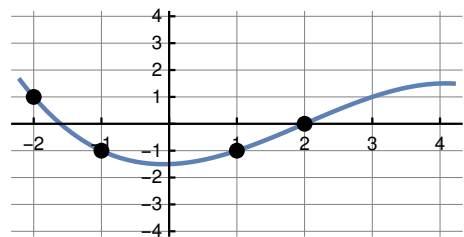
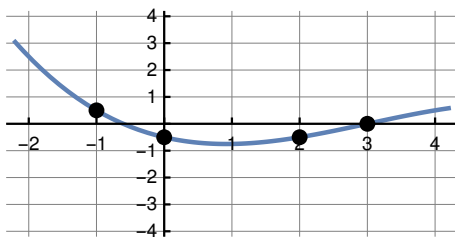
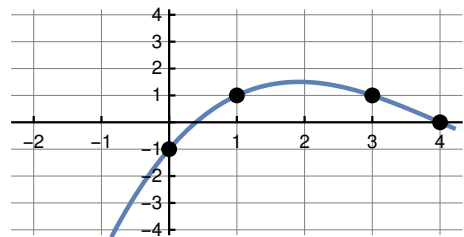
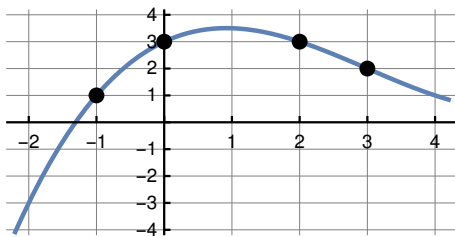
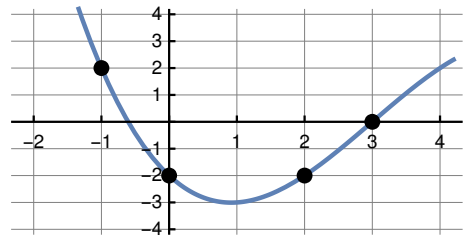
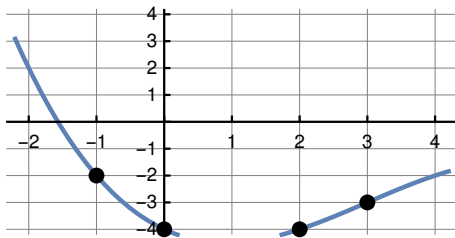


2. Consider the function $f(x)$, whose graph is given below. Note the points it goes through.



This question is about the functions $af(bx + c) + d$, for some numbers $a, b, c, d \in \mathbf{R}$.

- (a) What values of a, b, c, d give the original function $f(x)$?
 (b) Identify the values a, b, c, d for each function below that give the corresponding graph. The marked points above are also marked in each plot.



- (c) **Bonus:** If the point (p, q) lies on the graph of $f(x)$, what are the coordinates of this point on the graph of $af(bx + c) + d$?