Worksheet 13

21 February 2017

1. Warm up:

(a) What is a sequence? Give an example of a sequence.

(b) What is a series? Give an example of a series.

2. Find the first four terms in the following sequences, starting at n=1.

- (a) $x_n = 2n + 1$
- (b) $a_n = (-2)^n$
- (c) $b_n = 2 + (1-n)^n$
- (d) $c_n = 2c_{n-1} + c_{n-1}^2$ where $c_1 = 2$

3. Reindex the sequences above so that the term for n=1 previously is now for n=0.

4. Find a general formula for the nth term of the following sequences. The first term given in each sequence is for n = 1.

- (a) $16, 25, 36, 49, \dots$
- (b) $\frac{1}{2}, \frac{2}{3}, \frac{3}{4}, \dots$
- (c) $e, \frac{e}{\pi}, \frac{e^2}{\pi}, \frac{e^2}{\pi^2}, \frac{e^3}{\pi^2}, \dots$
- (d) $-1, 1, -1, 1, -1, 1, \dots$
- (e) $0, 1, 0, 1, 0, \dots$
- (f) $1, \frac{-1}{4}, \frac{1}{27}, \frac{-1}{256}, \dots$

5. Using the periodicity of the cosine function, find formulas for the sequence in part (d) using:

(a) cos

(b) | cos |