

23 April 2015

1. **Warm up:** Convert the coordinates on the left to polar  $(r, \theta)$  and the ones on the right to rectangular  $(x, y)$ .

(a)  $(0, 0)$ (f)  $(0, 0)$ (b)  $(1, 0)$ (g)  $(1, 0)$ (c)  $(0, 1)$ (h)  $(0, \pi)$ (d)  $(1, 1)$ (i)  $(1, \pi)$ (e)  $(55, 78.2)$ (j)  $(41/7, 22\pi/3)$ 

2. Consider the parametric curve  $(x, y) = (\pi \sin(t + \pi), \sin(t))$ .

(a) What is the length of the curve from  $t = 0$  to  $t = \pi/2$ ?

(b) Give the curve in rectangular coordinate form  $y = f(x)$ .

(c) Give the curve  $y = 5x$  as a parametric curve with  $x = \sin(t)$ .

3. Recall the Maclaurin series is the Taylor series centered at  $a = 0$ .

(a) Give the first three terms of the Maclaurin series of  $f(x) = 3e^{3x^2+2}$ .

(b) Give the first three terms of Maclaurin series of  $g(x) = \sin(2x - \pi) + 2$ .

(c) Give the second degree Maclaurin polynomial of  $f(x)g(x)$ .

(d) In the Maclaurin polynomial of  $f(x)g(x)$ , how many terms are added to get the coefficient of:

i.  $x^{20}$

ii.  $x^{21}$