

Discussion session 4 - 4 September 2014

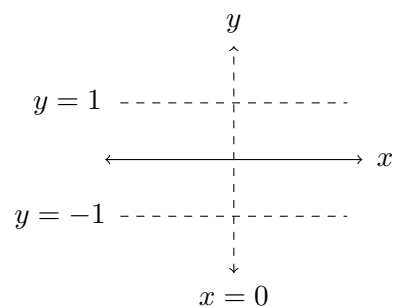
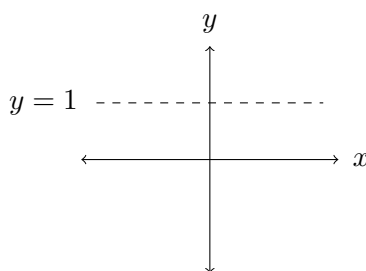
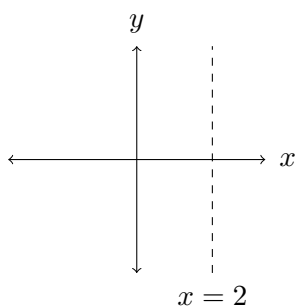
1. Consider the piecewise function below, and find $\lim_{x \rightarrow 2^\pm} [f(x)]$ and $\lim_{x \rightarrow 5^\pm} [f(x)]$.

$$f(x) = \begin{cases} 6x - 1 & \text{if } x \leq 2, \\ 3x^2 - x & \text{if } 2 < x \leq 5, \\ 2x^2 + 3x + 5 & \text{if } x > 5. \end{cases}$$

2. Calculate the limit

$$\lim_{x \rightarrow -\infty} \left[\frac{x^4 + x^3 + 1}{3x^4 + \sqrt{x^8 + 3}} \right].$$

3. Draw on the axes below the graph of three functions that have the indicated asymptotes.



4. Write down a formula for one of the graphs above. Redraw the graphs if necessary.