

1 September 2015

1. **Warm up:** Let $f(x)$ be a function with $f(1) = 10$ and $f(2) = -2$, and $h(x) = f(x + 1)$. Evaluate the following expressions:

- (a) $h(0)$
- (b) $h(1)/2$
- (c) $f\left(\sqrt{\ln(e^4)}\right)$
- (d) $f(h(f(2) + 3) + 3) + 3$

2. Evaluate the following limits, if they exist.

- (a) $\lim_{x \rightarrow 0} [\ln(x + 1)]$
- (b) $\lim_{x \rightarrow 1} \left[\frac{x^2 - 1}{x - 1} \right]$
- (c) $\lim_{y \rightarrow 4} \left[\frac{y^2 - y - 12}{\sqrt{y} - 2} \right]$
- (d) $\lim_{z \rightarrow 3} \left[\frac{3 - z}{z - 3} \right]$
- (e) $\lim_{w \rightarrow 3} \left[\frac{|w - 3| + |w - 3|}{w - 3} \right]$

3. Consider the following function:

$$f(x) = \begin{cases} 2x^3 & \text{if } x \leq -1, \\ ax + b & \text{if } -1 < x < 1, \\ |x| & \text{if } x \geq 1. \end{cases}$$

- (a) Find a pair of real numbers a, b that make the function f continuous.
 - (b) With the pair you found in part (a), graph f on a grid.
 - (c) For any real number r , what is $\lim_{x \rightarrow r} [f(x)]$ equal to? In other words, how can you simplify this given limit expression?
4. Let $f(x) = \sin(1/x)$.
- (a) What is the domain of f ?
 - (b) What is the range of f ?
 - (c) What is $\lim_{x \rightarrow \infty} [f(x)]$, if it exists?
 - (d) What is $\lim_{x \rightarrow 0} [f(x)]$, if it exists?
 - (e) Graph $f(x)$.